

Motivation of this Research

- ◆ Snakes perform many kinds of movement that are adaptable to a given environment **by changing locomotion modes**



Move on **soft ground**

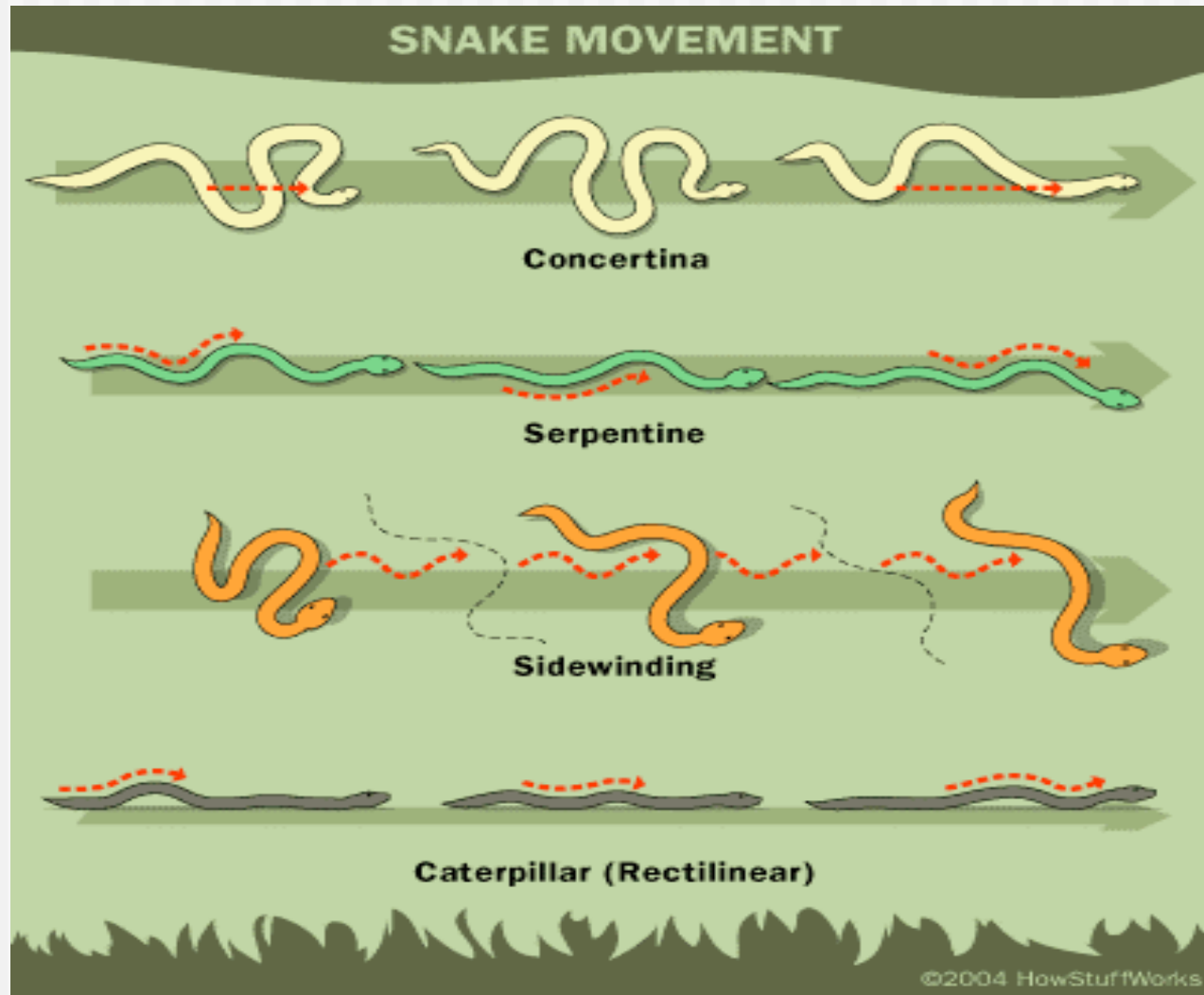


Move across **branches**

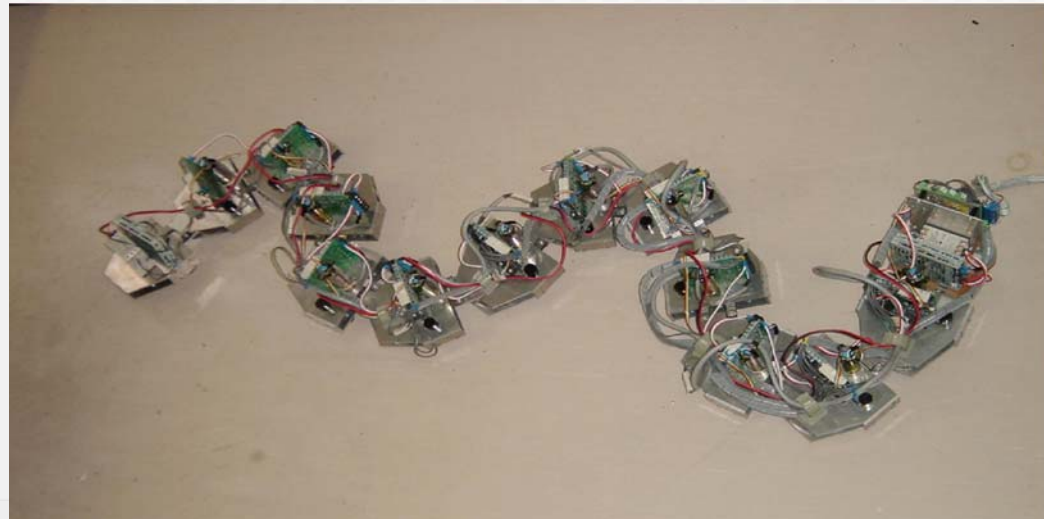
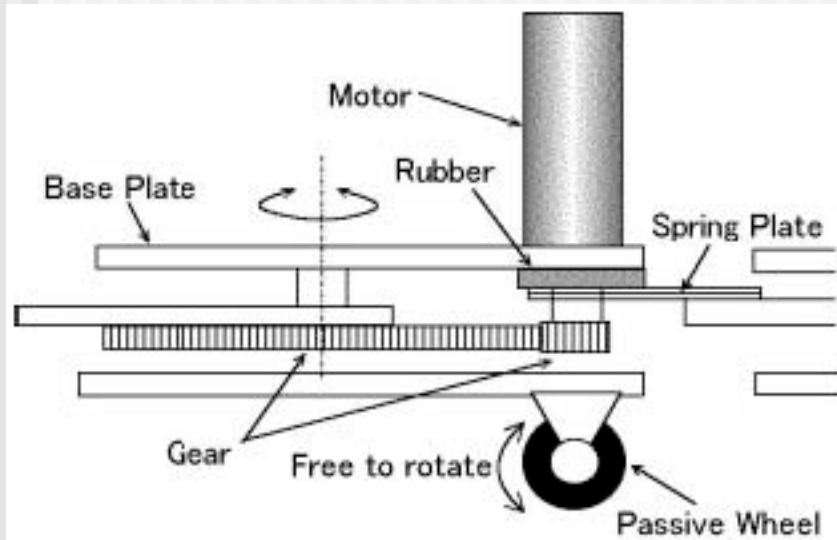
Snake robots are potentially superior for operations in highly constrained and unusual environments encountered in applications:

- Inspection of nuclear reactor cores and chemical sampling of buried toxic waste
- Space applications such as exploration of planetary surfaces and planet sample return mission
- Rescue task like searching of victims in the debris after a disaster
- Underwater applications such as ocean exploration and oil field service

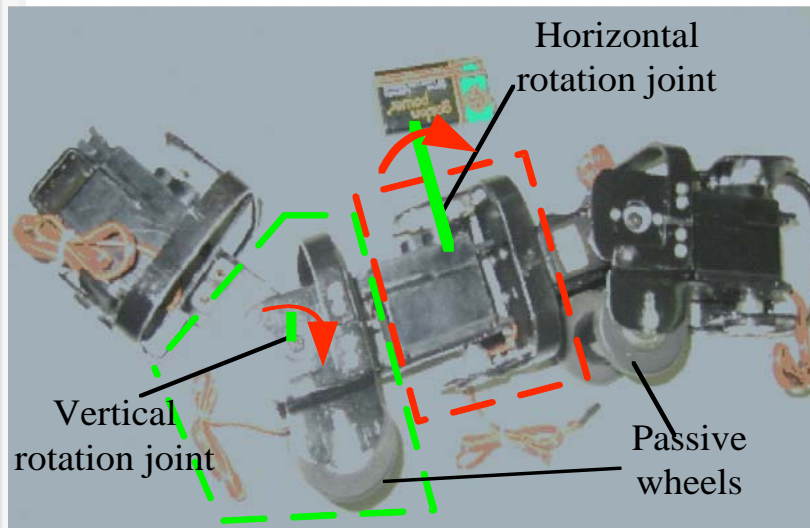
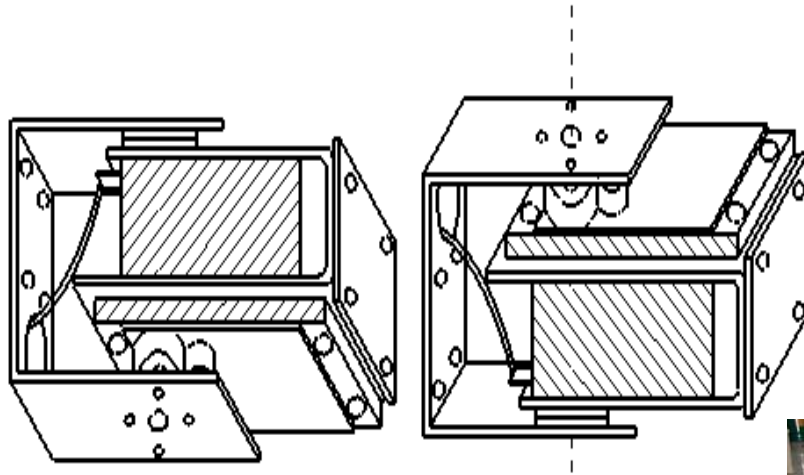
Motion Examples of Snakes



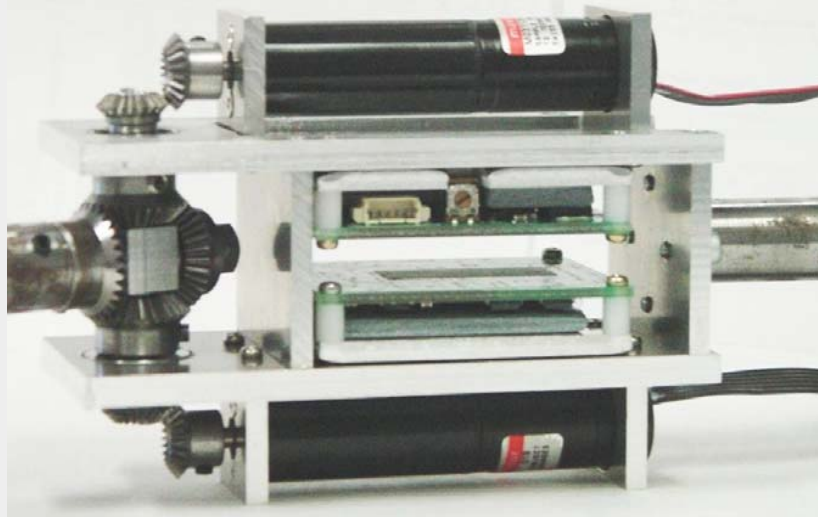
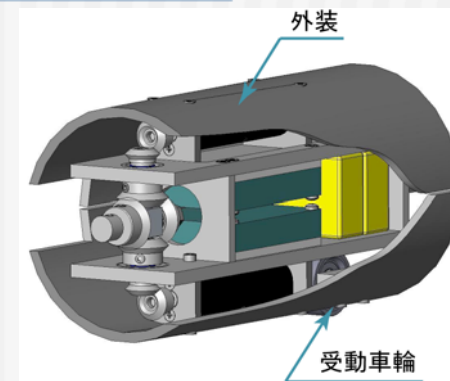
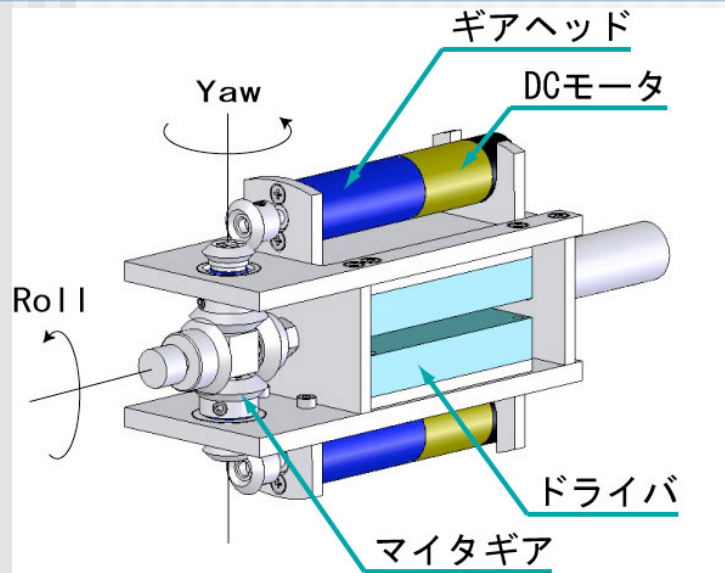
Design of 2D Snake Robot (1 DOF Joint)



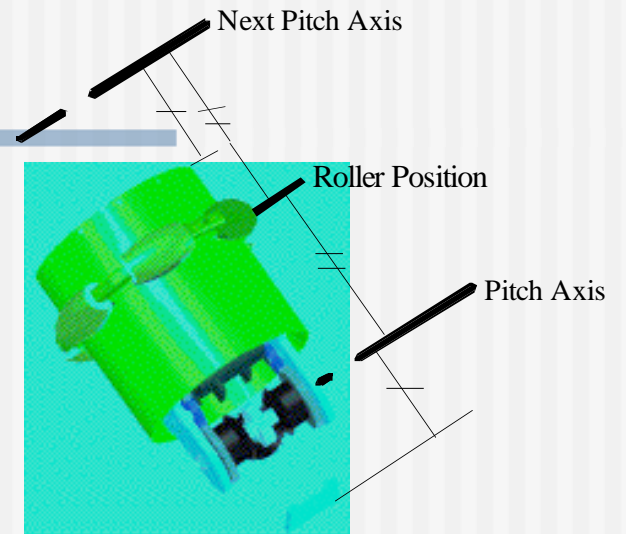
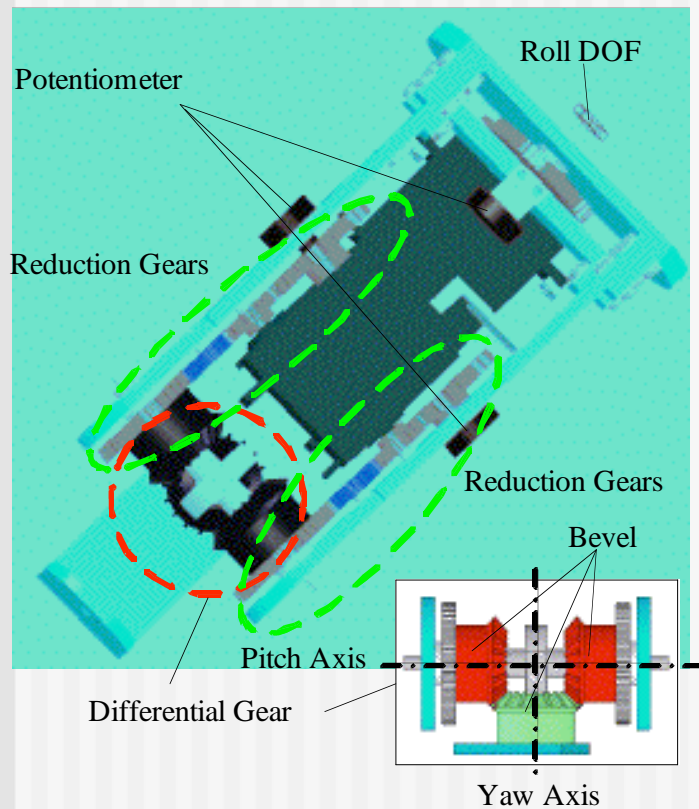
Design of 3D Snake Robot (1 DOF Joint)



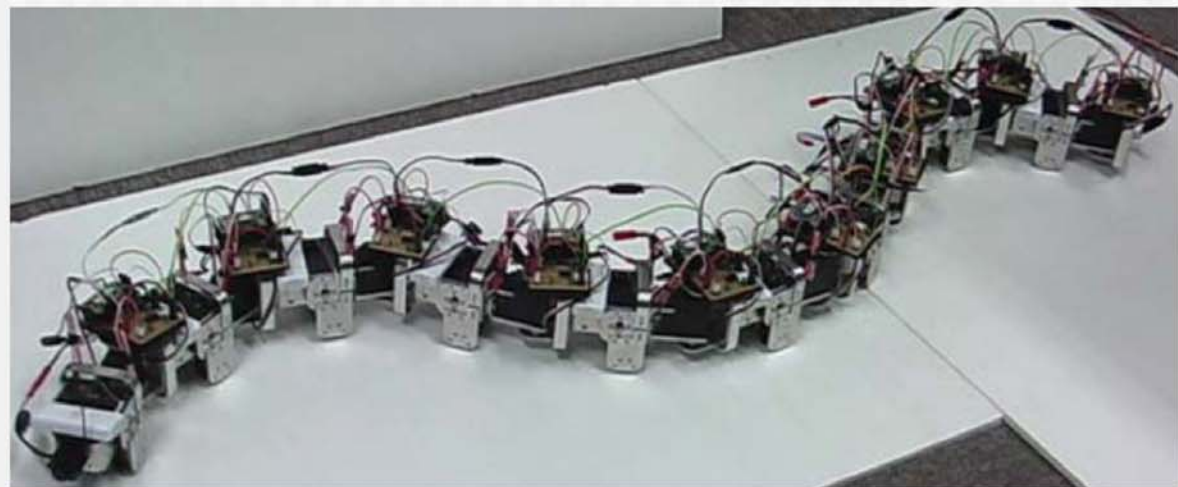
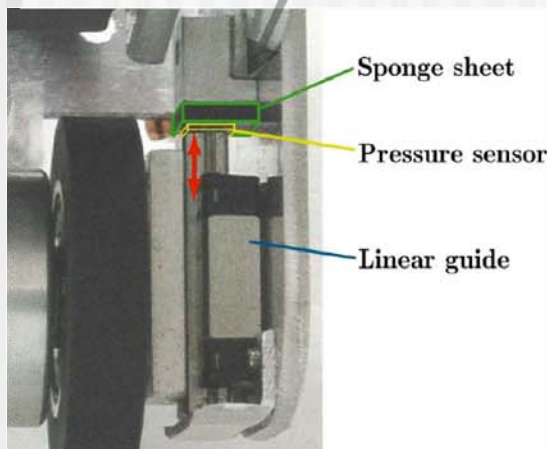
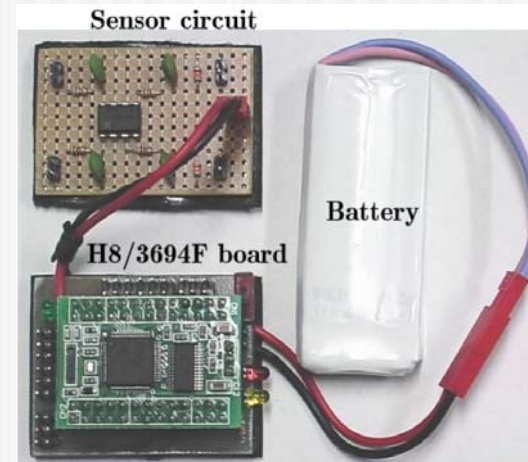
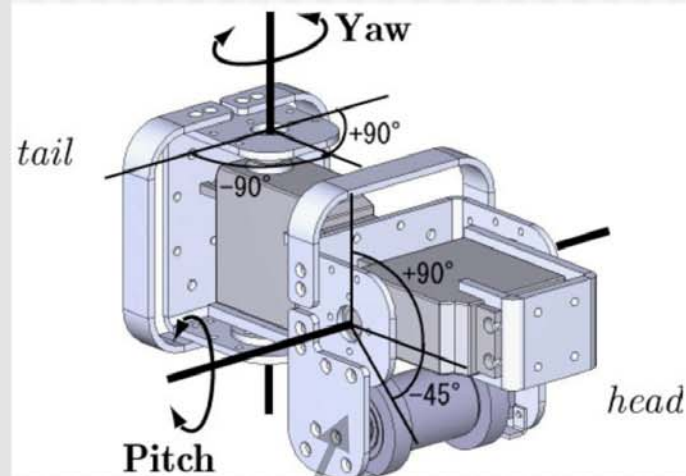
Design of 3D Snake Robot (2 DOF Joint)



Design of 3D Snake Robot (3 DOF Joint)



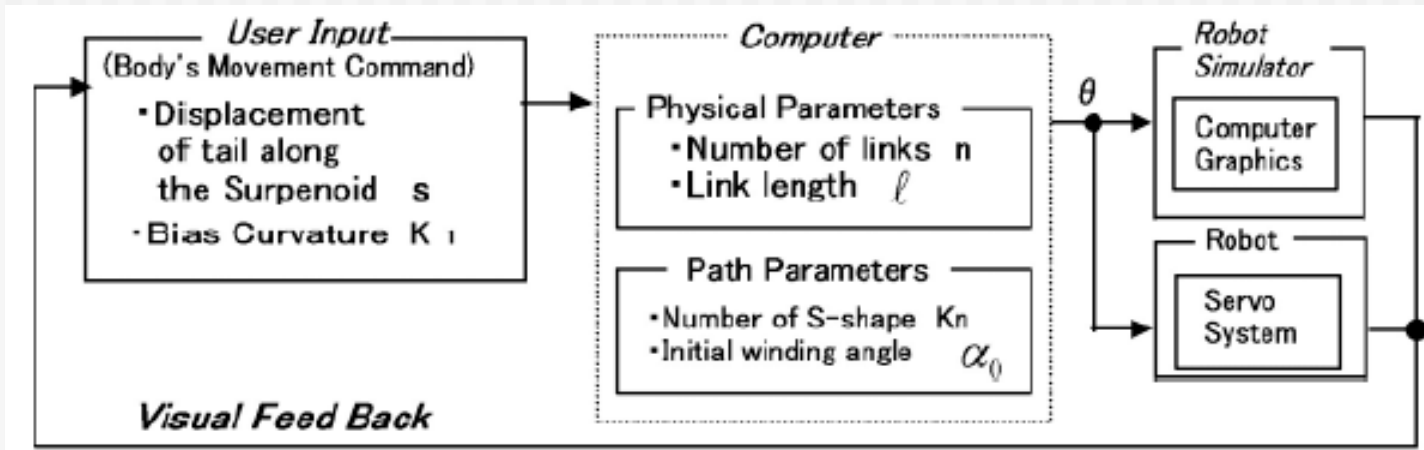
Design of 3D Snake Robot for Environmental Adaptation



Control of Snake Robots

- Analytical model of body dynamics for known environment
- Rhythmic motion generated by neural oscillator networks

Control System of 2D Motion of Snake Robots



Serpentine :

$$\begin{bmatrix} \theta_i^y(s) \\ \theta_i^p(s) \end{bmatrix} = \begin{bmatrix} -2\alpha_0^y \sin\left(\frac{K_n\pi}{n}\right) \sin\left(\frac{2K_n\pi}{L}s + \frac{2K_n\pi}{n}i\right) \\ 0 \end{bmatrix}$$



Sinusoidal :

$$\begin{bmatrix} \theta_i^y(s) \\ \theta_i^p(s) \end{bmatrix} = \begin{bmatrix} 0 \\ -2\alpha_0^p \sin\left(\frac{K_n\pi}{n}\right) \sin\left(\frac{2K_n\pi}{L}s + \frac{2K_n\pi}{n}i\right) \end{bmatrix}$$



Control System of 3D Motion of Snake Robots

Sinus-lifting :

Wavelength:	Phase Difference:
Yaw:Pitch=1:2	$-\pi/2$

$$\begin{bmatrix} \theta_i^y(s) \\ \theta_i^p(s) \end{bmatrix} = -2 \begin{bmatrix} \alpha_0^y \sin\left(\frac{K_n \pi}{n}\right) \sin\left(\frac{2K_n \pi}{L} s + \frac{2K_n \pi}{n} i\right) \\ \alpha_0^p \sin\left(\frac{2K_n \pi}{n}\right) \sin\left(\frac{4K_n \pi}{L} s + \frac{4K_n \pi}{n} i - \frac{\pi}{2}\right) \end{bmatrix}$$

Sidewinding :

Wavelength:	Phase Difference:
Yaw:Pitch=1:1	$-\pi$

$$\begin{bmatrix} \theta_i^y(s) \\ \theta_i^p(s) \end{bmatrix} = -2 \sin\left(\frac{K_n \pi}{n}\right) \begin{bmatrix} \alpha_0^y \sin\left(\frac{2K_n \pi}{L} s + \frac{2K_n \pi}{n} i\right) \\ \alpha_0^p \sin\left(\frac{2K_n \pi}{L} s + \frac{2K_n \pi}{n} i - \pi\right) \end{bmatrix}$$



Analysis of Creeping Locomotion

- Analysis of snake creeping locomotion

Elucidated the standard creeping movement form of a snake through analyzing physiologically

- Analysis of creeping locomotion of snake-like robot

The number of *S*-shape does not give large influence on the performance, but the initial winding angle largely does

- Analysis of creeping locomotion of snake-like robot on slopes

- ▲ The case that, the number of *S*-shape = 2, is better used for our 12-link snake-like robot

- ▲ The unsymmetrical body shape is better used to improve the robot's performance on the slope

Control of Snake Robots

- Analytical model of body dynamics for known environment
- Rhythmic motion generated by neural oscillator networks

Rhythmic motion generated by neural oscillator networks

Biologically:

Rhythmic locomotion of animals:

Generated by neural oscillator networks located in spinal cord

- Construction of models

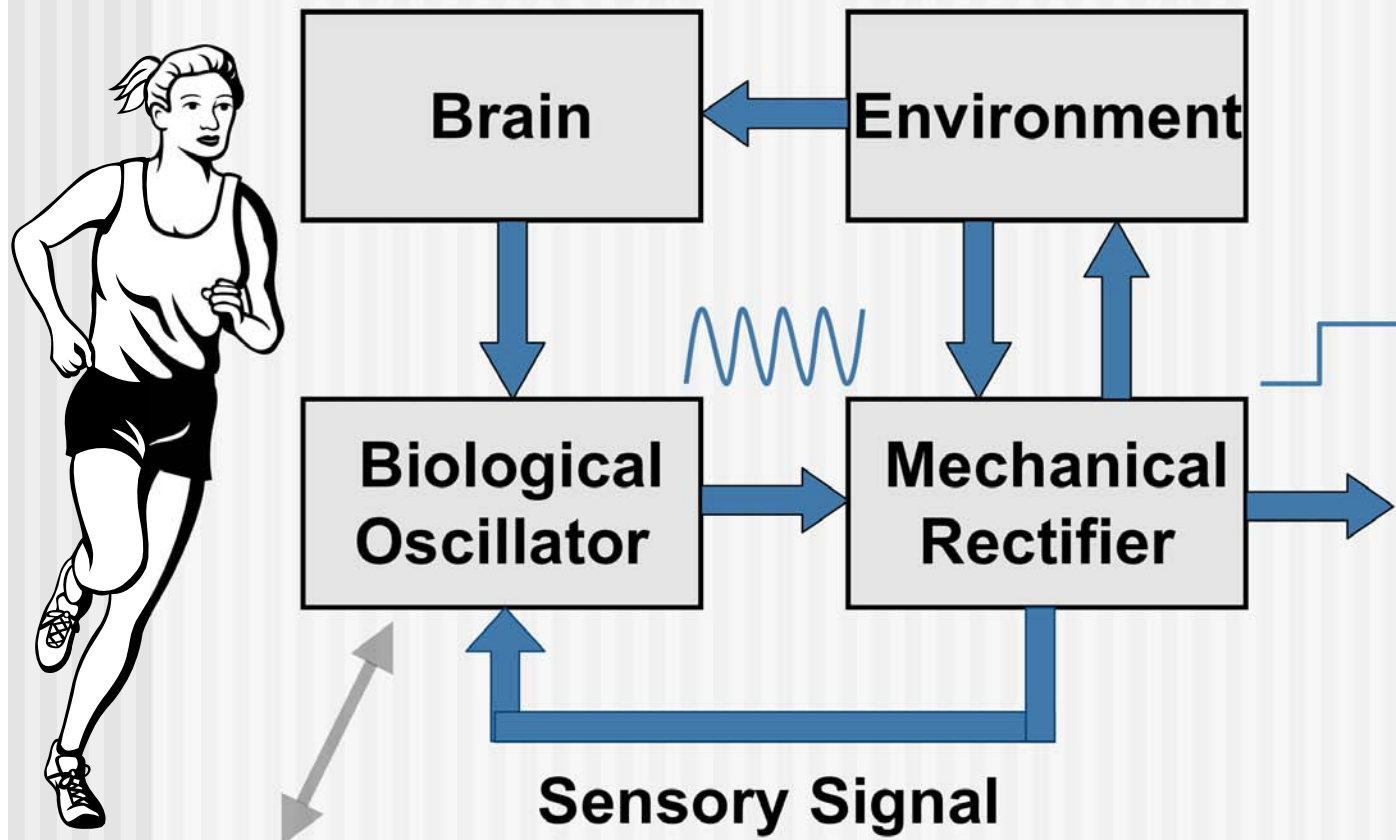
Engineering:

Biologically-inspired Robots:

Needs for Adaptive Controllers for Rhythmic Motion

- Application of neural oscillator network model

Biological Control for Locomotion



Neural Oscillator network

Snake-like Robots

Special Features:

- Many units connected in series
- Interact with environments only through friction
- **Rhythmic locomotion**



- Difficulty in calculating body dynamics
(large DOF, complex interaction with environment)
- Difficulty to generate purposive motion
in dynamic or unknown environment



Decentralized Control by Neural Oscillator Network

Snake-like Robots

Analytical model of body dynamics
for known environment

Computational complexity, lower adaptability



Rhythmic motion generated by
neural Oscillator networks

Lower computation, fast adaptation

Matsuoka's Neural Model

Characteristics:

- Mutually inhibiting neurons
- Fatigue effect in each neuron

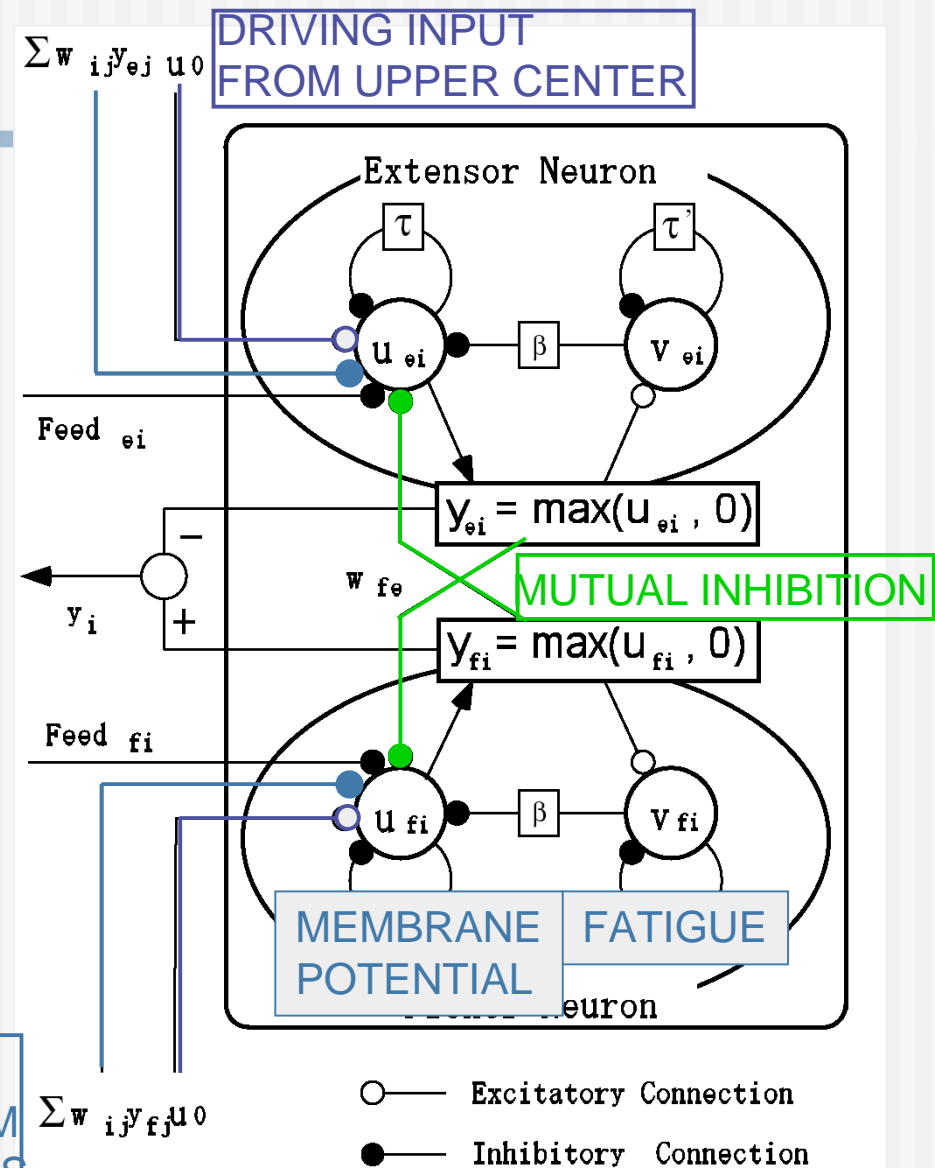
$$\tau \dot{u}_{\{e,f\}i} = -u_{\{f,e\}i} + w_{fe} y_{\{f,e\}i} - \beta v_{\{e,f\}i} + u_{0,\{e,f\}i} + \text{Feed}_{\{e,f\}i} + \sum_{j=1}^n w_{ij} y_{\{e,f\}j}$$

$$y_{\{e,f\}i} = \max(0, u_{\{e,f\}i})$$

$$\tau' \dot{v}_{\{e,f\}i} = -v_{\{e,f\}i} + y_{\{e,f\}i}$$

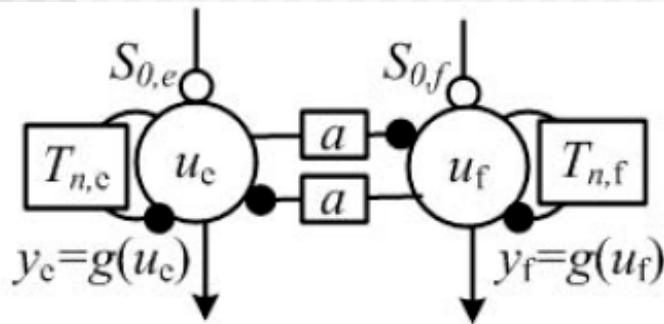
$$y_i = y_{fi} - y_{ei}$$

EXCITATION OR INHIBITION FROM OTHER NEURONS

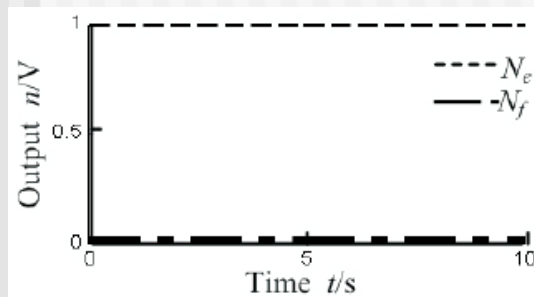


CPG model by Matsuoka

Properties of Mutual Inhibitory CPG Model (without FATIGUE)



(a) Structure



(b) Output of the neurons

$$T_{n,e}\dot{u}_e + u_e = s_{0,e} - ag(u_f)$$

$$T_{n,f}\dot{u}_f + u_f = s_{0,f} - ag(u_e)$$

$$y_{\{e,f\}} = g(u_{\{e,f\}}), g(u_{\{e,f\}}) = \max(0, u_{\{e,f\}})$$

$$c_out = y_e - y_f$$

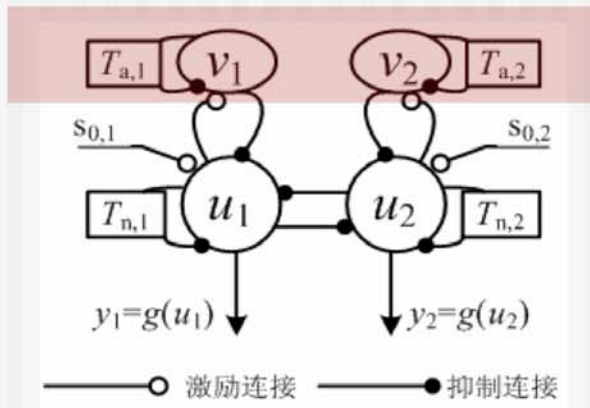
STATIONARY SOLUTIONS		
Conditions	Stationary states(u_1, u_2)	Stability
$s_{0,1} < 0, s_{0,2} > 0$	$(s_{0,1} - as_{0,2}, s_{0,2})$	Stable
$s_{0,1} > 0, s_{0,2} < 0$	$(s_{0,1}, s_{0,2} - as_{0,1})$	Stable
$s_{0,1} < 0, s_{0,2} < 0$	$(s_{0,1}, s_{0,2})$	Stable

STATIONARY SOLUTIONS		
Conditions	Stationary states(u_1, u_2)	Stability
$a < S$	$(\frac{s_{01} - a s_{02}}{1 - a^2}, \frac{s_{02} - a s_{01}}{1 - a^2})$	Stable
$s < a < S, s_1 > s_2$	$(s_1, s_2 - a s_1)$	Stable
$s < a < S, s_1 < s_2$	$(s_1 - a s_2, s_2)$	Stable
$a > S$	$(\frac{s_{01} - a s_{02}}{1 - a^2}, \frac{s_{02} - a s_{01}}{1 - a^2})$	Unstable
	$(s_1, s_2 - a s_1)$	Stable
	$(s_1 - a s_2, s_2)$	Stable

$$S = \max\{s_e, 1/s_f, s_f/s_e\}$$

The Mutual Inhibitory CPG Model without “Fatigue” never yield any oscillatory behavior

Properties of Mutual Inhibitory CPG Model (with FATIGUE)



$$T_{n,i}\dot{u}_i + u_i = s_{0,i} - a g(u_j) - \beta v_i$$

$$T_{a,i}\dot{v}_i + v_i = y_i$$

$$T_{n,i}\dot{u}_i + u_i = s_{0,i} - a g(u_j) - \beta v_i$$

$$T_{a,i}\dot{v}_i + v_i = y_i$$

$$y_i = g(u_i) \quad g(u_i) = \max(0, u_i) \quad i = 1, 2$$

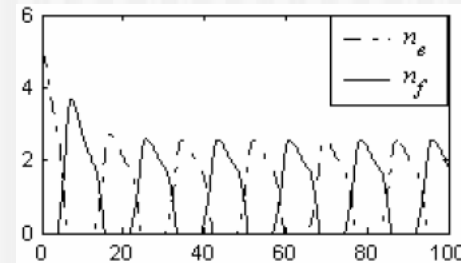
Theorem 1: No stable stationary solution, if and only if

$$\begin{aligned} a' &< s \\ a &> 1 + \frac{T_n}{T_a} \end{aligned}$$

where

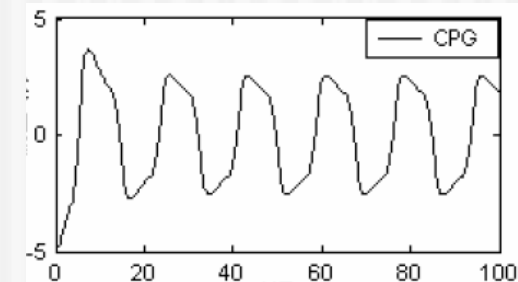
$$a' = a/(1+\beta), \quad s = \min(s_{0,1}/s_{0,2}, s_{0,2}/s_{0,1})$$

Theorem 2: Any solutions are bounded for $t > 0$ while $a \geq 0$.



(a)
Output of neurons

(b)
Output of CPG



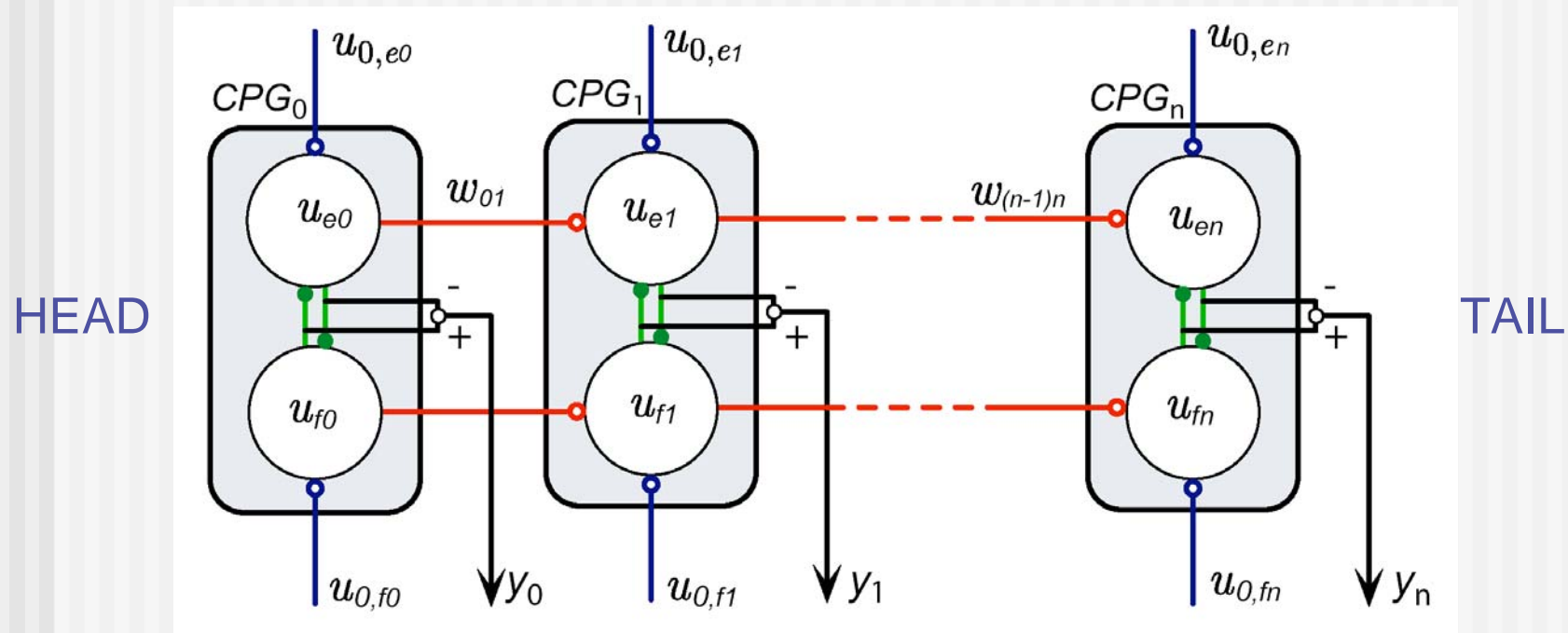
The Mutual Inhibitory CPG Model with “Fatigue” yield oscillatory behavior

Network Structure

One-way excitatory connection from head to tail

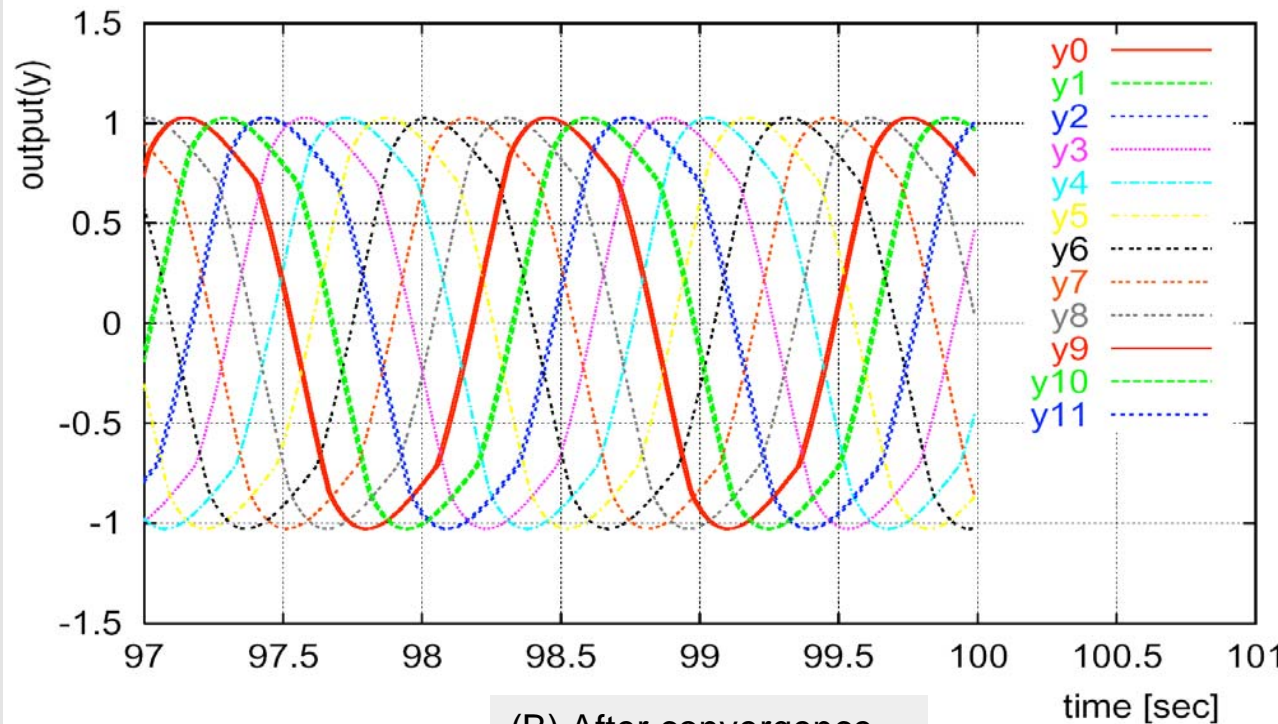


Propagation of undulation with specific phase difference



CPG network

Neural Oscillator Simulation



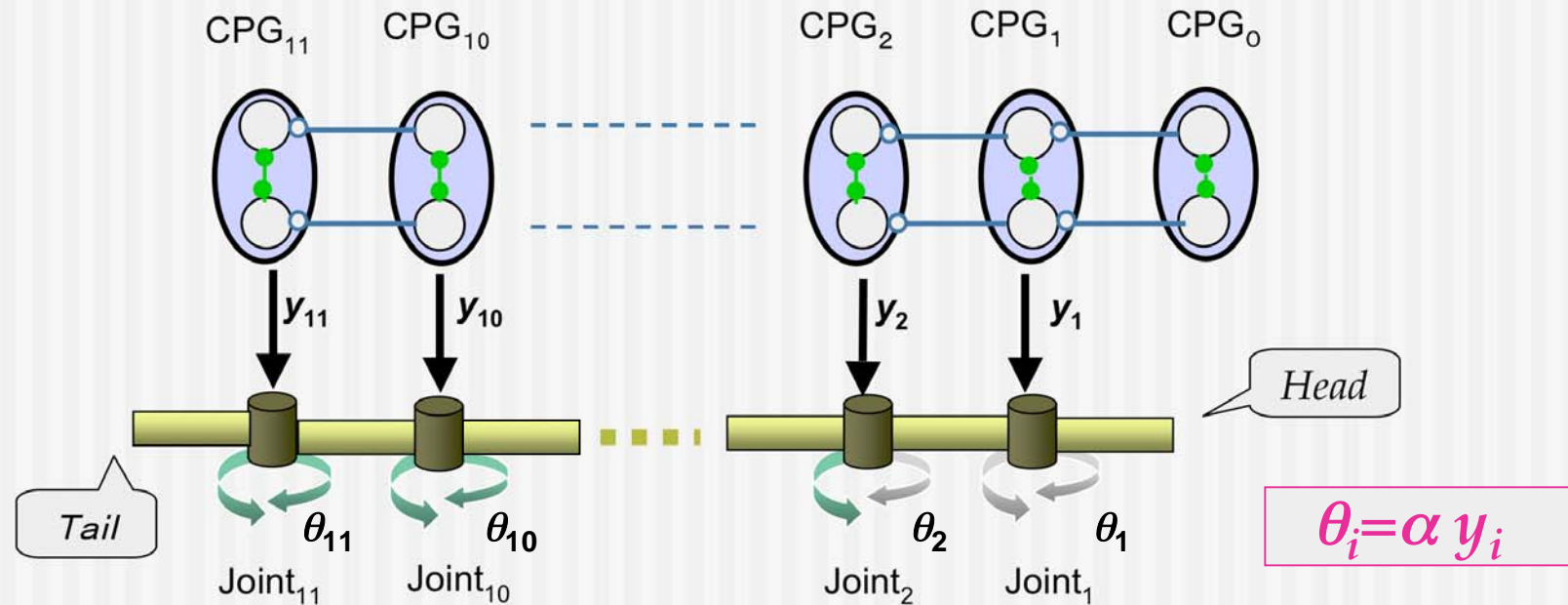
(B) After convergence

Parameters	Value
$U_{0\{e,\beta\}}(U_{0\{e,\beta\}i})$ ($i=1\dots 11$)	3.55(3.0)
t	0.2
t'	1.0
b	5.0
W_{fe}	-1.2
W_{ji}	0.2
cycle[s]	1.3
Phase Difference	45°

(set by trial-and-error)

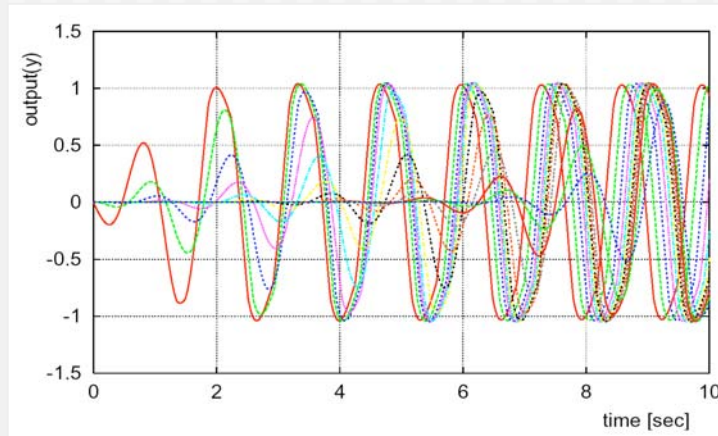
After 35 seconds, all CPGs oscillate with 1.3[s] cycle with 45[deg] phase difference

Implementation to Snake Robot

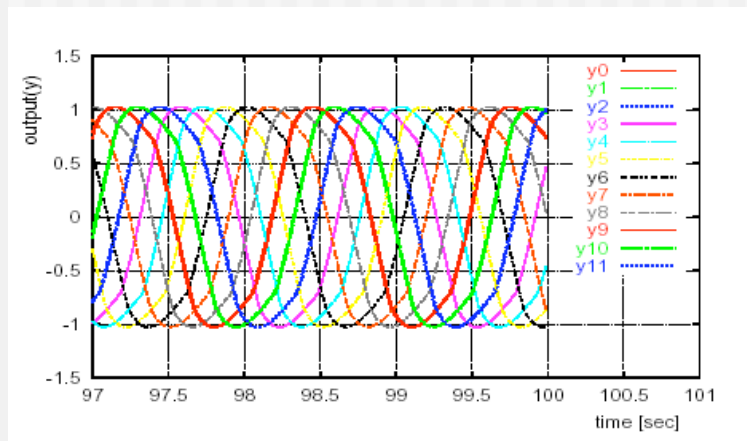


- Output of CPGs are input to joint as angle
- CPG₀ is used as a driving input to the network

Simulation Result



Initial stage

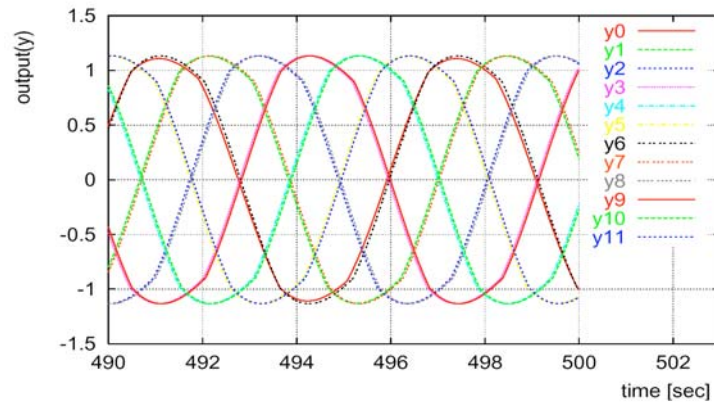


After convergence

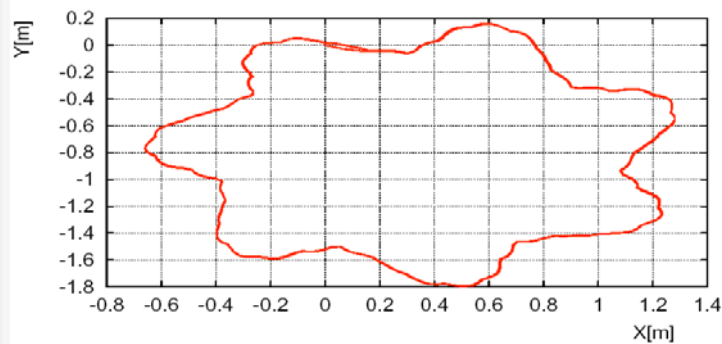
Parameters	Value
$u_{0\{e,f\}0}(u_{0\{e,f\}i}) (i=1 \dots 12)$	3.55(3.0)
t	0.2
t'	1.0
b	5.0
w_{fe}	-1.2
w_{ji}	0.2
Cycle [s]	1.3
Phase difference [deg]	45°

(set by trial-and-error)

Simulation Result



Steady stage



Curvature

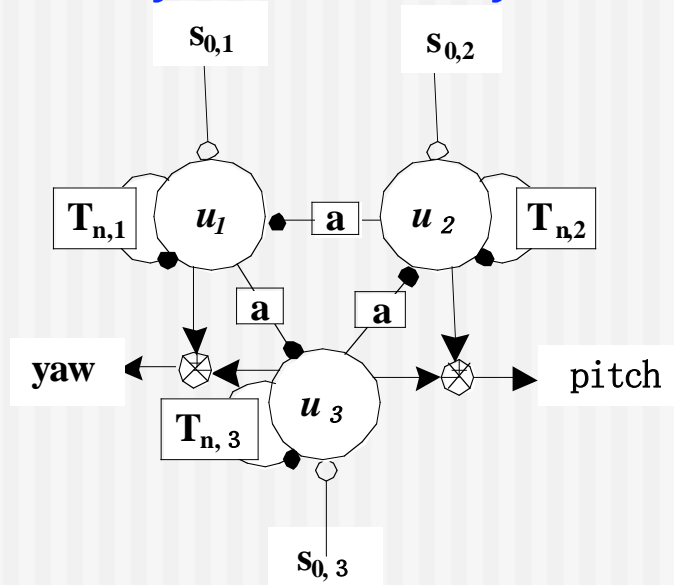
Parameters	Value
$u_{0\{e,f\}0}(u_{0\{e,f\}i})$ ($i=1 \dots 12$)	11.7(9.7)
t	2.0
t'	10.0
b	20.0
w_{fe}	-1.2
w_{ji}	0.2
Cycle [s]	7.0
Phase difference [deg]	60°

(set by trial-and-error)

A New Neural Model (1)

(Cyclic Inhibitory CPG Model)

Unilateral Cyclic Inhibitory CPG Model



$$T_{n,1}u_1 + u_1 = s_{0,1} - ag(u_2)$$

$$T_{n,2}u_2 + u_2 = s_{0,2} - ag(u_3)$$

$$T_{n,3}u_3 + u_3 = s_{0,3} - ag(u_1)$$

$$y_i = g(u_i), g(u_i) = \max(0, u_i) \quad i = 1, 2, 3$$

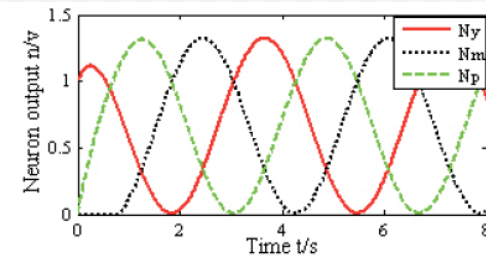
$$y_{out} = y_1 - y_3$$

$$p_{out} = y_2 - y_3$$

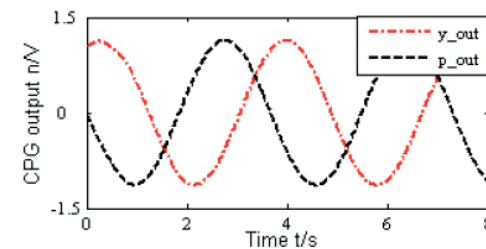
Theorem 1: Under the condition $T_{n,1}=T_{n,2}=T_{n,3}=\tau$ and $s_{0,1}=s_{0,2}=s_{0,3}=0$, the equations have no stable stationary solution, if and only if

$$a \geq 2 \text{ or } a \leq -1.$$

Theorem 2: Any solutions of the equations are bounded for $t > 0$ under the condition $a \geq 0$.



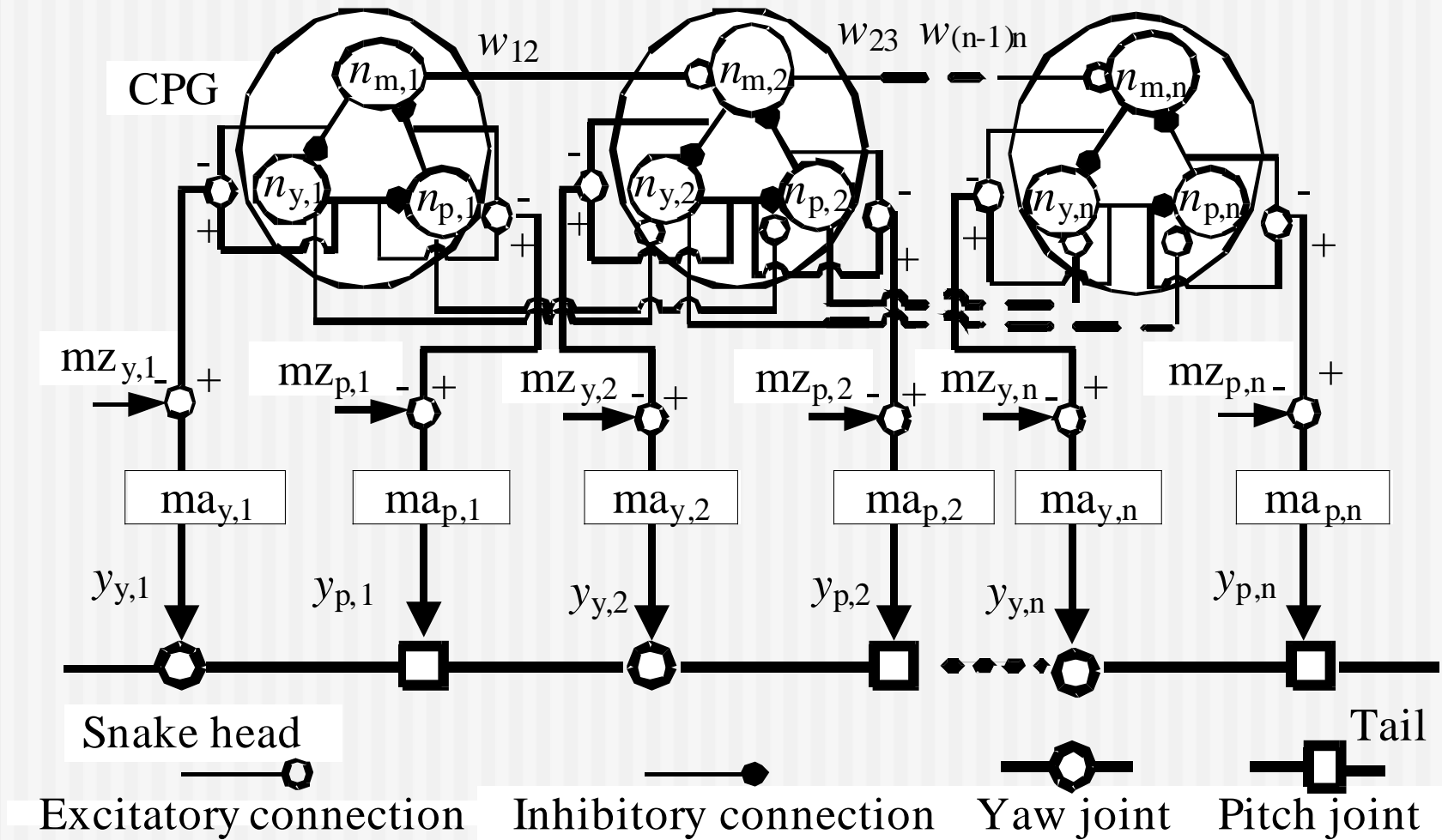
(a) Output of the neurons



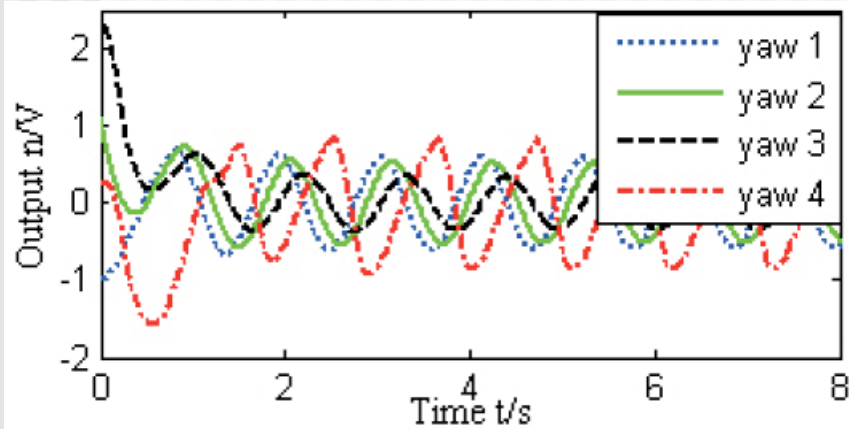
(b) Output of the cyclic inhibitory CPG

Fig. 5. Step response ($T_{n,1} = T_{n,2} = T_{n,3} = 1$, $s_{0,1} = s_{0,2} = s_{0,3} = 1$, $a = 2$)

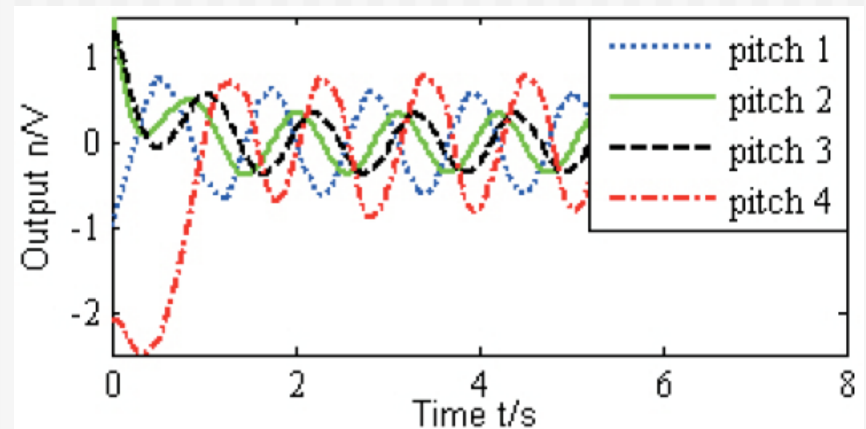
Network Structure and Implementation to Snake Robot



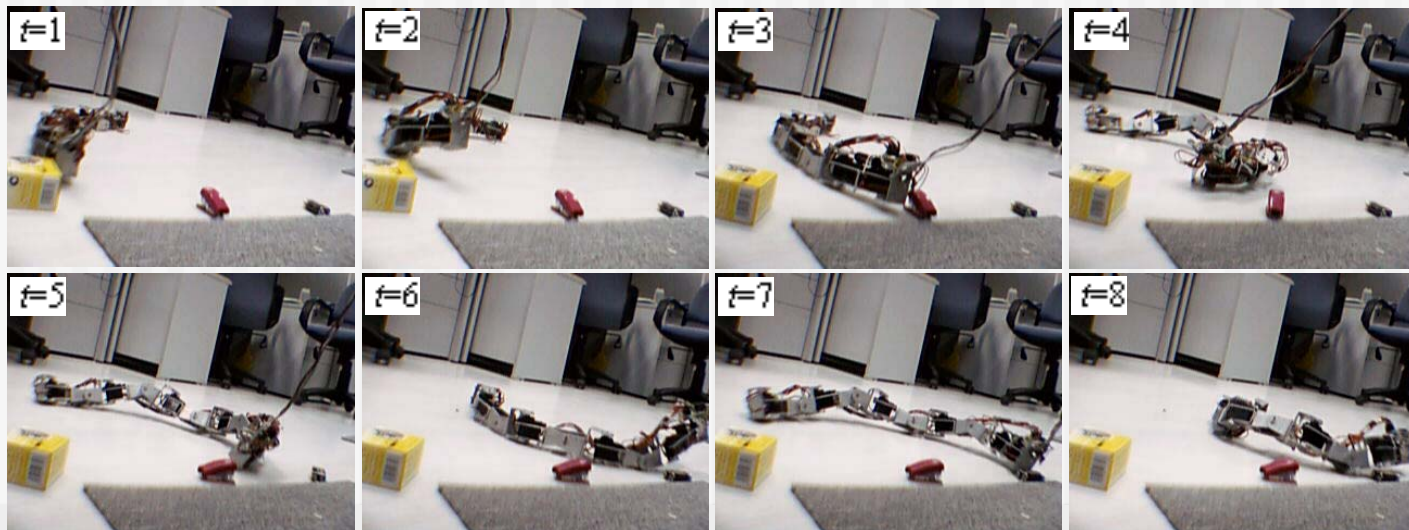
Simulation Result



(a) Yaw joint signal



(b) Pitch joint signal



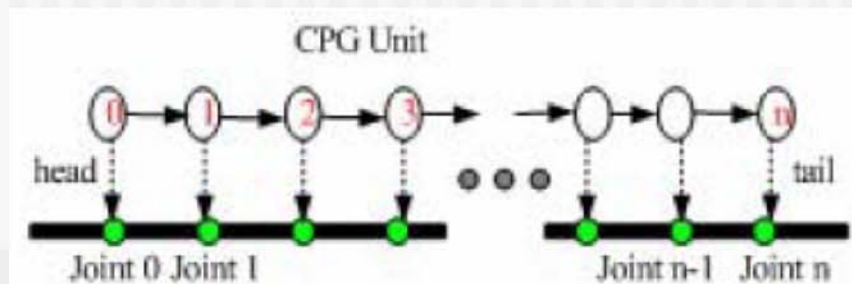
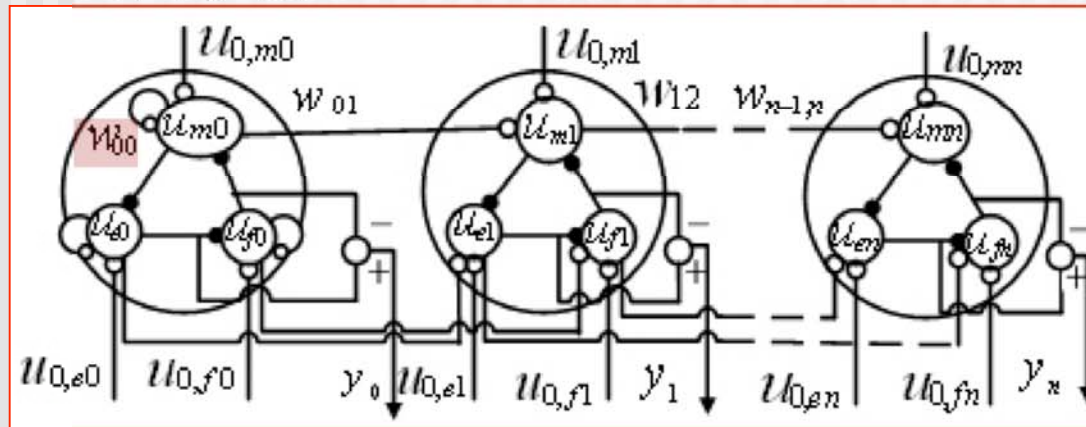
Unilateral Cyclic Inhibitory CPG Model for Serpentine motion of Snake-like Robots

$$\tau \dot{u}\{e, f, m\}_i = -u\{e, f, m\}_i + w\{e, f, m\}_i y\{m, e, f\}_i - \beta v\{e, f, m\}_i + u_0\{e, f, m\}_i + \text{Feed}\{e, f, m\}_i$$

$$y\{e, f, m\}_i = \max(0, u\{e, f, m\}_i)$$

$$\tau \dot{v}\{e, f, m\}_i = -v\{e, f, m\}_i + y\{m, e, f\}_i$$

$$y_i = y_{fi} - y_{ei}$$



No pitch, only Yaw
→ Serpentine Motion

Conditions for a stable oscillation:

$$w\{e\}/(1+\beta) \geq (\mu_0\{m\} - \text{Feed}\{m\} - \sum w_{ij}y_j\{m\}) / (\mu_0\{e\} - \text{Feed}\{e\} - \sum w_{ij}y_j\{e\})$$

$$w\{e\} \geq 1 + \tau / \tau'$$

$$w\{m\}/(1+\beta) \geq (\mu_0\{f\} - \text{Feed}\{f\} - \sum w_{ij}y_j\{f\}) / (\mu_0\{m\} - \text{Feed}\{m\} - \sum w_{ij}y_j\{m\})$$

$$w\{m\} \geq 1 + \tau / \tau'$$

$$w\{f\}/(1+\beta) \geq (\mu_0\{e\} - \text{Feed}\{e\} - \sum w_{ij}y_j\{e\}) / (\mu_0\{f\} - \text{Feed}\{f\} - \sum w_{ij}y_j\{f\})$$

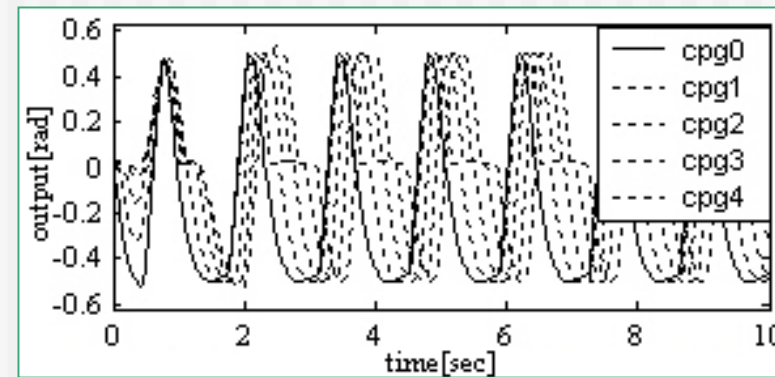
$$w\{f\} \geq 1 + \tau / \tau'$$

$$w_{ij} = \begin{cases} w_0 & \text{if } i = j - 1 \\ 0 & \text{others} \end{cases}$$

Realization of Serpentine Motion by Unilateral Cyclic Inhibitory CPG Model



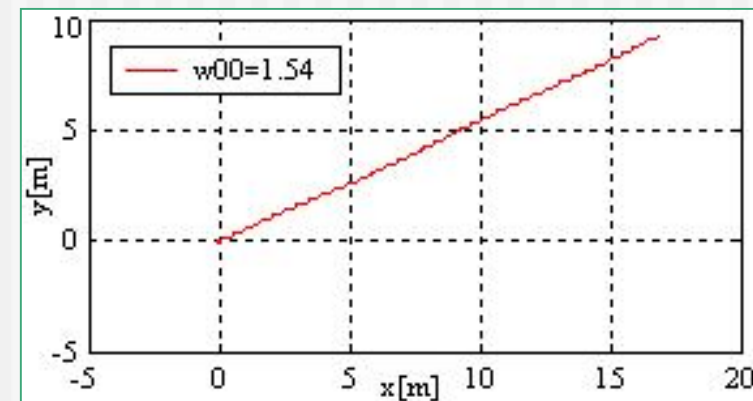
Output curve of CPG



MAIN PARAMETERS OF THE CPG MODEL

Driving input $\mu_0(e, f, m)_i$ ($i=0, \dots, n-1$)	25
Time constant for state τ	03
Time constant for fatigue τ'	03
Fatigue coefficient β	1
Head-neuron connection weight w_{00}	1.54
Inter-CPG connection weight w_0	15
Inter-neuron connection weight $w_{(e, f, m)_i}$ ($i=1, \dots, n-1$)	25

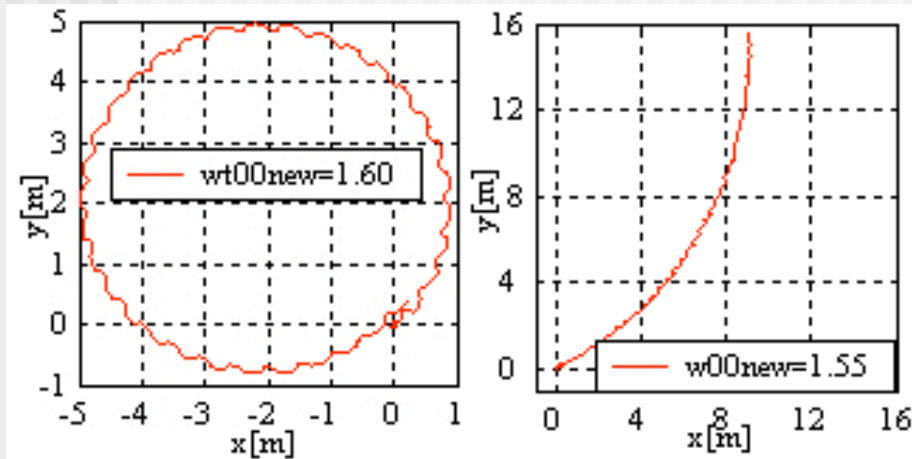
Head trajectory of the robot



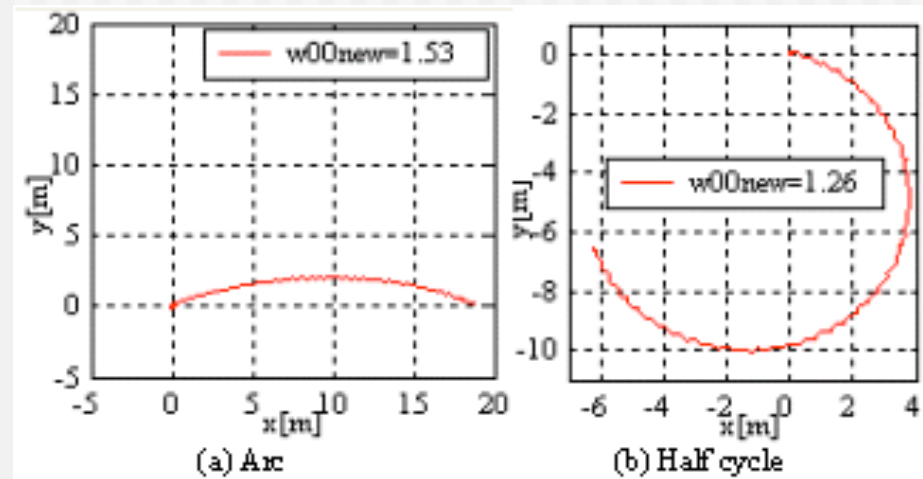
CPG Parameters for Turn Motions

$$W_{00new} = W_{00} + \Delta W_{00}$$

$$\underline{W_{00}=1.54}$$



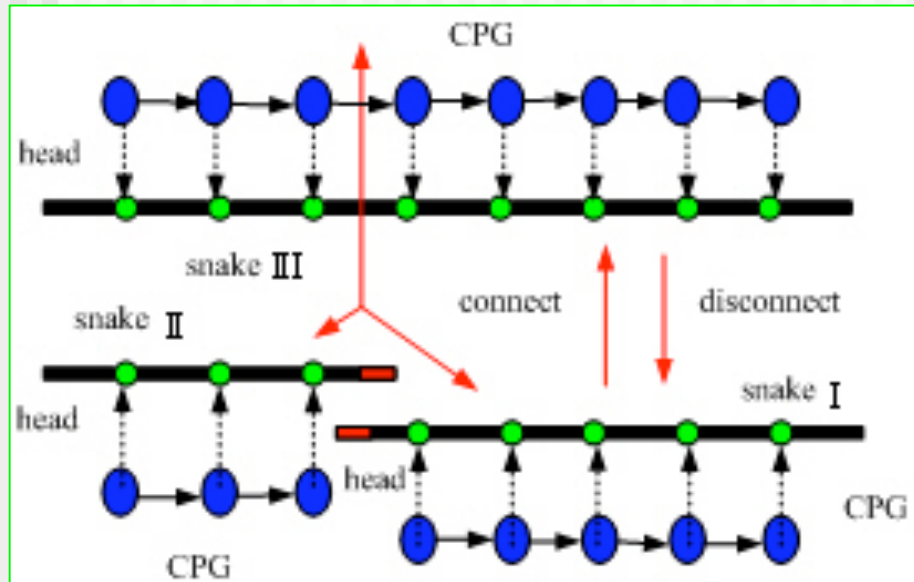
Left-turn motion



Right-turning motion

- 1) $\Delta W_{00} > 0$, turns left (anti-clockwise)
 - 2) $\Delta W_{00} < 0$, turns right (clockwise)
- ◆ $|\Delta W_{00}|$ becomes smaller, turn motion angle become smaller

CPG Parameters for Reconfiguration

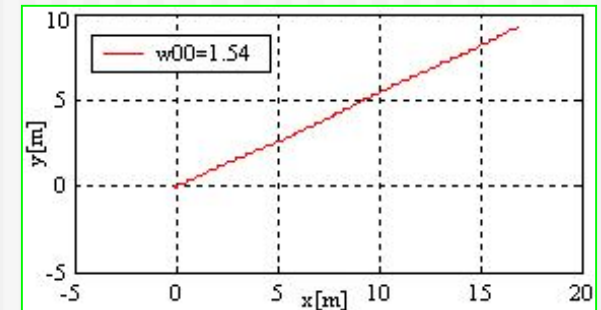


THE PARAMETERS OF THE CPG MODEL

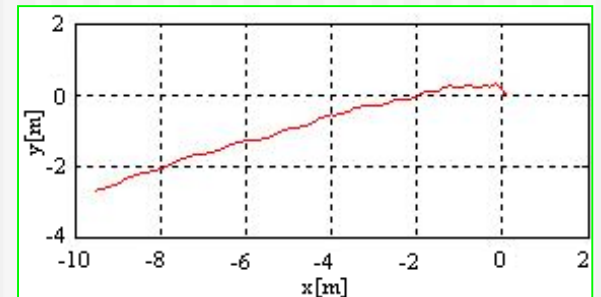
	Model I	Model II	Model III
w_{00}	1.54	0.1	-0.1
w_0	1.5	10	0.3

Head trajectories

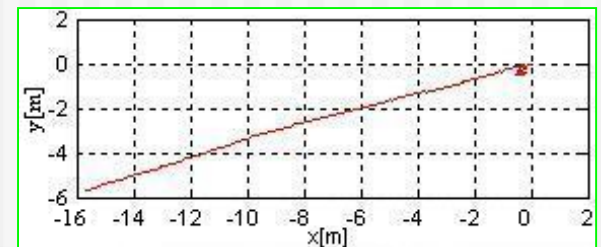
Model I



Model II



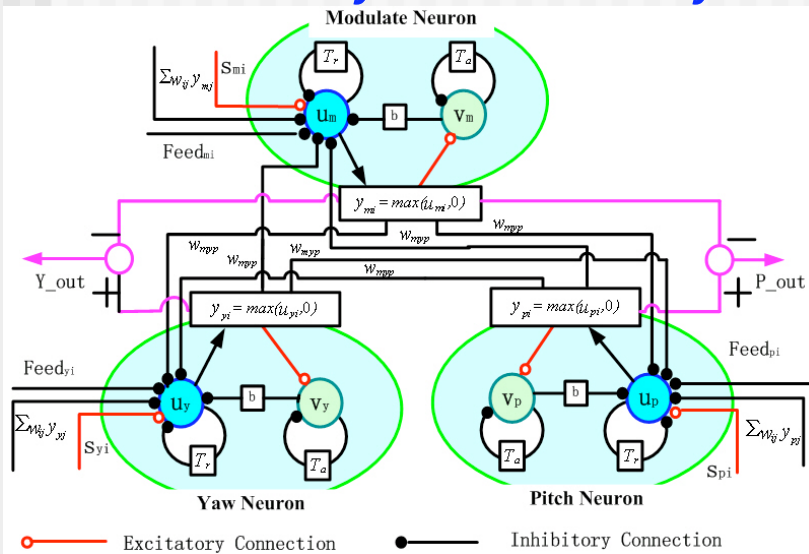
Model III



A New Neural Model (2)

(Cyclic Inhibitory CPG Model)

Bidirectional Cyclic Inhibitory CPG Model



Theorem 1: A solution of equations exists uniquely for any initial state and is bounded for $t > 0$.

Theorem 2: The equations have at least one stationary solution.

Conditions for a stable oscillation:

$$\frac{w_{ypm}}{1+b} \leq \min\left(\frac{\sin\{y,p,m\},t}{\sin\{p,m,y\},t}, \frac{\sin\{y,p,m\},t}{\sin\{m,y,p\},t}, \frac{\sin\{p,m,y\},t}{\sin\{m,y,p\},t}\right),$$

$$\frac{\sin\{p,m,y\},t}{\sin\{y,p,m\},t}, \frac{\sin\{m,y,p\},t}{\sin\{y,p,m\},t}, \frac{\sin\{m,y,p\},t}{\sin\{p,m,y\},t}.$$

$$w_{ypm} > 1 + \frac{T_r}{T_a}.$$

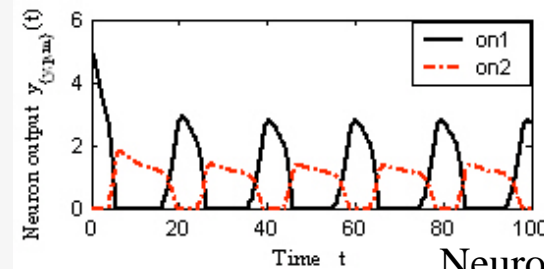
$$T_n, \{y,p,m\},i \dot{u}_{\{y,p,m\},i} = -u_{\{y,p,m\},i} - w_{\{y,p,m\},i} v_{\{p,m,y\},i} - w_{\{y,p,m\},i} v_{\{m,y,p\},i} - \beta v_{\{y,p,m\},i} + s_{0,\{y,p,m\},i} + Feed_{\{y,p,m\},i} + \sum_{j=1}^n w_{ij} y_{\{y,p,m\},j}$$

$$T_a, \{y,p,m\},i \dot{v}_{\{y,p,m\},i} = -v_{\{y,p,m\},i} + y_{\{y,p,m\},i}$$

$$y_{\{y,p,m\},i} = g(u_{\{y,p,m\},i}), g(u_{\{y,p,m\},i}) = \max(0, u_{\{y,p,m\},i})$$

$$y_{yaw,i} = y_{y,i} - y_{m,i}$$

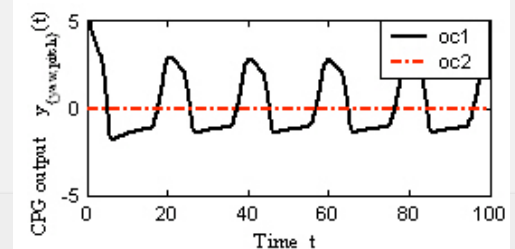
$$y_{pitch,i} = y_{p,i} - y_{m,i}$$



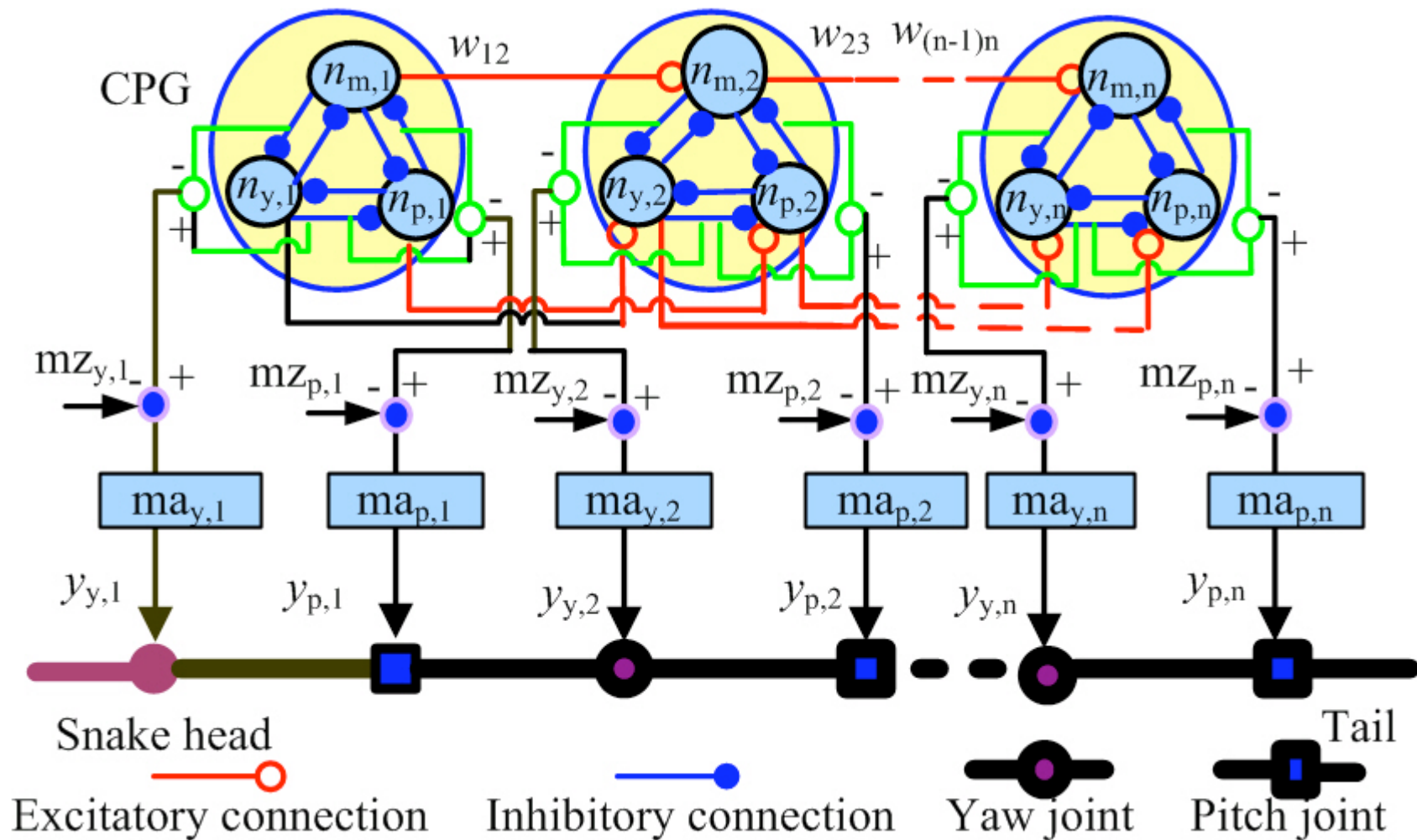
(a)

Neuron output in a CPG

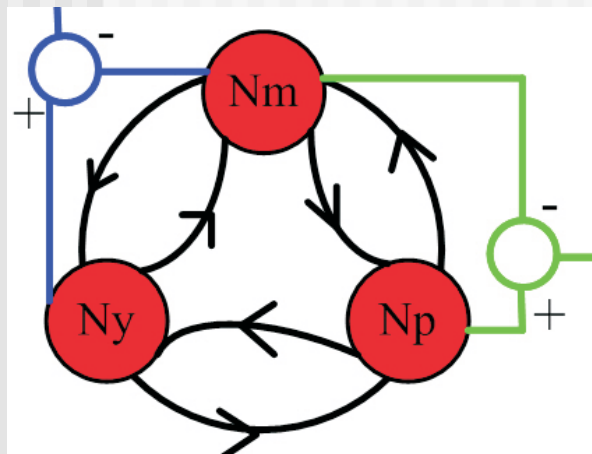
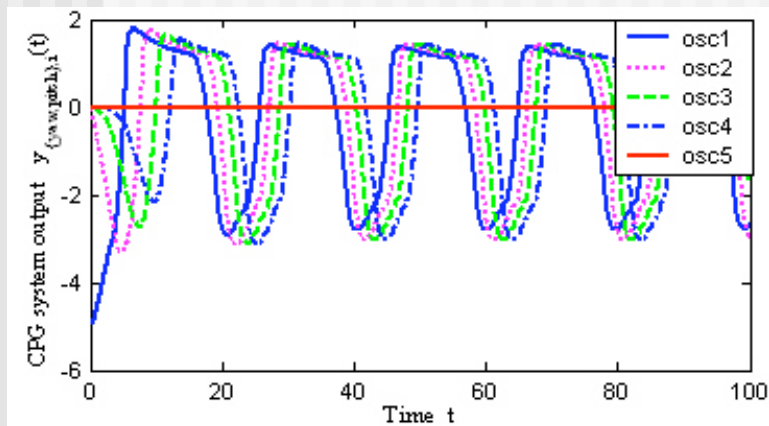
(b)
CPG output



Network Structure and Implementation to Snake Robot



Simulation Result



[Y1,P1,M1]



[**1**,0,0]: Serpentine



[0,**1**,0]: Concertina



[0,0,**1**]: Sidewinding